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"Challenges are what make life interesting and overcoming them is what makes life meaningful"  
 -Joshua J. Marine

HW: "Exponential Growth and Decay" w/s #1-11 odd, 12

AIM: What is Exponential Growth and Decay ?

Warm Up:

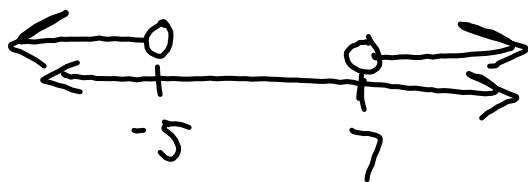
1)

Express the solution in set builder, and interval notation:  $x^2 - 22 > 13 + 2x$   
 $-2x - 13 - 13 - 2x$

$$x^2 - 2x - 35 > 0 \quad \begin{matrix} \text{open} \\ \text{(positives)} \end{matrix} \quad \text{GO L I}$$

$$(x-7)(x+5) > 0$$

$$\begin{matrix} 7 & -5 \end{matrix}$$



SB:  $\{x \mid x < -5 \text{ or } x > 7\}$

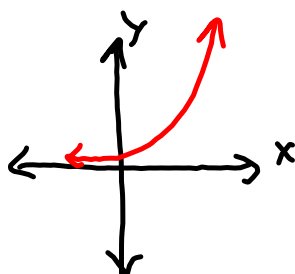
Int:  $(-\infty, -5) \cup (7, \infty)$

I.  $f(x) = ab^x$  is an exponential function where  $b$  is called the base

### Exponential Growth

ex.  $f(x) = 2^x$ .

$b > 1$

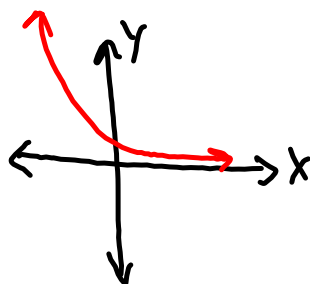


⊗ Asymptote  
 $y = 0$

### Exponential Decay

Ex.  $f(x) = \left(\frac{1}{2}\right)^x$ .

$0 < b < 1$



Asymptote:  $y = 0$

Label each of the following as exponential growth, or decay:

1)  $f(x) = 3^x$  **G**

2)  $f(x) = .2^x$  **D**

3)  $f(x) = 5.7^x$  **G**

4)  $f(x) = \left(\frac{22}{7}\right)^x$  **G**

5)  $f(x) = 3^{-x}$   
 $f(x) = \left(\frac{3}{1}\right)^{-x}$

$f(x) = \left(\frac{1}{3}\right)^x$

**Decay**

6)  $f(x) = 77^{-x}$   
 $f(x) = \left(\frac{1}{77}\right)^x$

**Decay**

Asymptote: A value that a function gets closer to, but never touches.

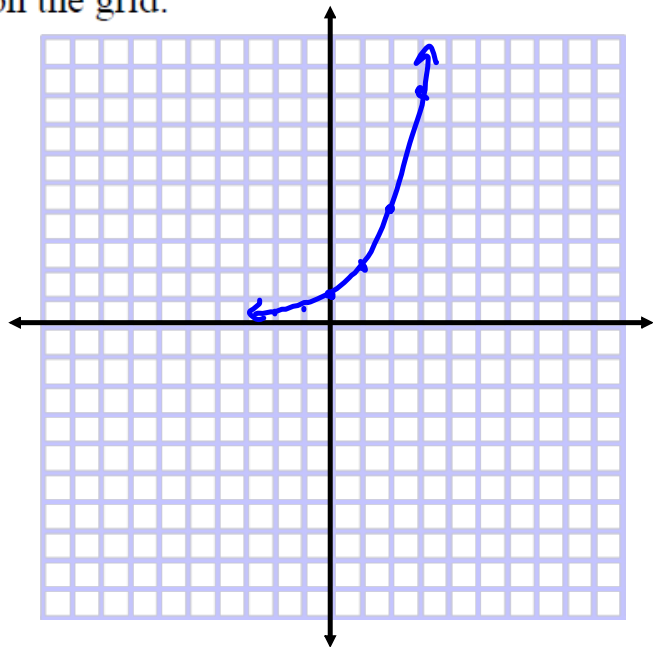
II.

1. Sketch the graph of  $f(x) = 2^x$  on the grid:

Table of values:

$$f(x) = 2^x$$

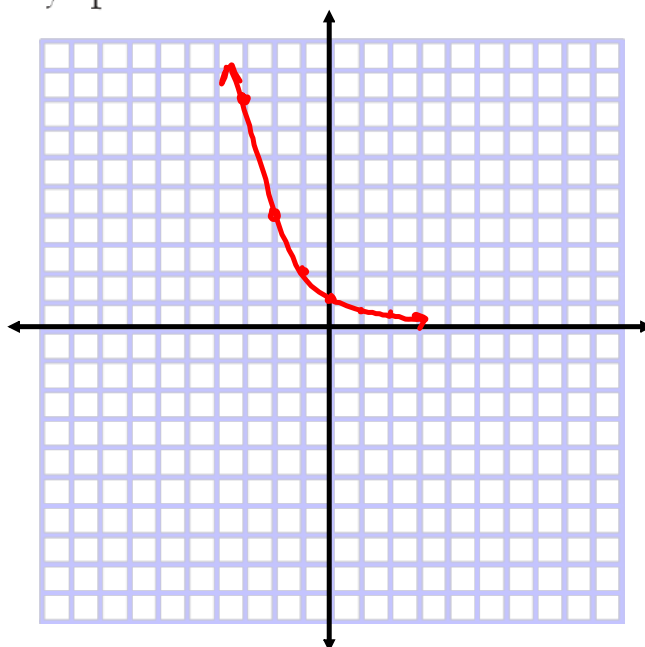
x	y
-2	$\frac{1}{4}$
-1	$\frac{1}{2}$
0	1
1	2
2	4
3	8



2. The graph of the equation  $y = \left(\frac{1}{2}\right)^x$  has an asymptote. On the grid below, sketch  $y = \left(\frac{1}{2}\right)^x$  and write the equation of this asymptote.

x	y
-3	8
-2	4
-1	2
0	1
1	$\frac{1}{2}$
2	$\frac{1}{4}$

Asymptote:  
 $y = 0$



III. Applications for exponential growth and decay. A very popular base is  $e$ .

1) Inspect the graph of  $f(x) = e^x$ .

The base  $e$  is used in calculating **compound interest**, which you will study in detail later.

2) Here is an example involving **compound interest**.

Matt places \$1,200 in an investment account earning an annual rate of 6.5%, compounded continuously. Using the formula  $V = Pe^{rt}$ , where  $V$  is the value of the account in  $t$  years,  $P$  is the principal initially invested,  $e$  is the base of a natural logarithm, and  $r$  is the rate of interest, determine the amount of money, to the *nearest cent*, that Matt will have in the account after 10 years.

$V$  = Final value

$P$  = Starting Amount

$r$  = interest rate

$t$  = time

$V = ?$

$P = 1200$

$r = 6.5\% = .065$

$t = 10 \text{ years}$

$V = Pe^{rt}$

$$V = 1200e^{(.065)(10)}$$

$$V = \$2298.65$$

$$\text{Growth} = P \left(1 + \frac{r}{n}\right)^{nt}$$

$$\text{Decay} = P \left(1 - \frac{r}{n}\right)^{nt}$$

- 4) A radioactive substance has an initial mass of 100 grams and its mass halves every 4 years. Which expression shows the number of grams remaining after  $t$  years?

(1)  $100(4)^{\frac{t}{4}}$

(3)  $100\left(\frac{1}{2}\right)^{\frac{t}{4}}$

Decay  
 $100\left(\frac{1}{2}\right)^{\frac{t}{4}}$

(2)  $100(4)^{-2t}$

(4)  $100\left(\frac{1}{2}\right)^{4t}$

- 6) Mr. Carman can drum 910 single strokes in one minute. Each year, the number of single strokes he can play decreases by 1%. Which function models this situation? (Use  $t$  for years)

(1)  $f(x) = 910\left(\frac{99}{100}\right)^t$

(3)  $f(x) = 910\left(\frac{1}{100}\right)^t$

(2)  $f(x) = 910^t$

(4)  $f(x) = \text{yes}$

- 8) The graph of  $f(x)$  is constantly decreasing, but it will never actually achieve a value of zero. Which **behavior** does  $f(x)$  model?

(1) exponential growth

(3) a craving for *cheeze-it's*

(2) exponential decay

(4) relationship breakup denial

- 10) Mr. Carman's bunny making machine has gone hay-wire. It is creating bunnies at a rate that can be modeled by the equation  $B(x) = 5(2)^x$ , where  $x$  is the number of minutes since he turned the machine on, and  $B(x)$  is the number of bunnies.

a] How many bunnies will Mr. Carman have after 4 minutes?

b] **THINK:** How many bunnies did Mr. Carman start out with?

